

# Advanced Diffusion MRI

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# Overview

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- Introduction to Tractography
- Advanced Modelling:
  - Probabilistic Modelling
  - Multiple-fibre models
  - Diffusion MRI and microstructure

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- Hands on session

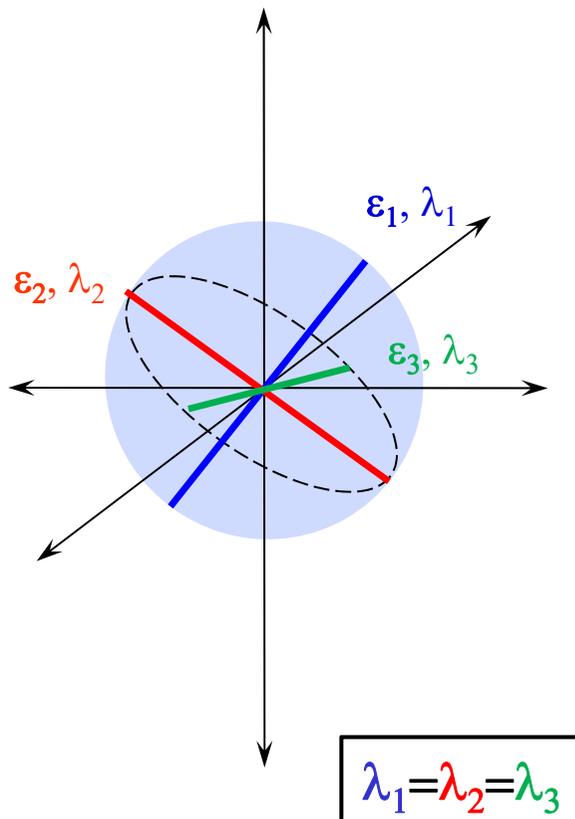
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# Introduction to Tractography

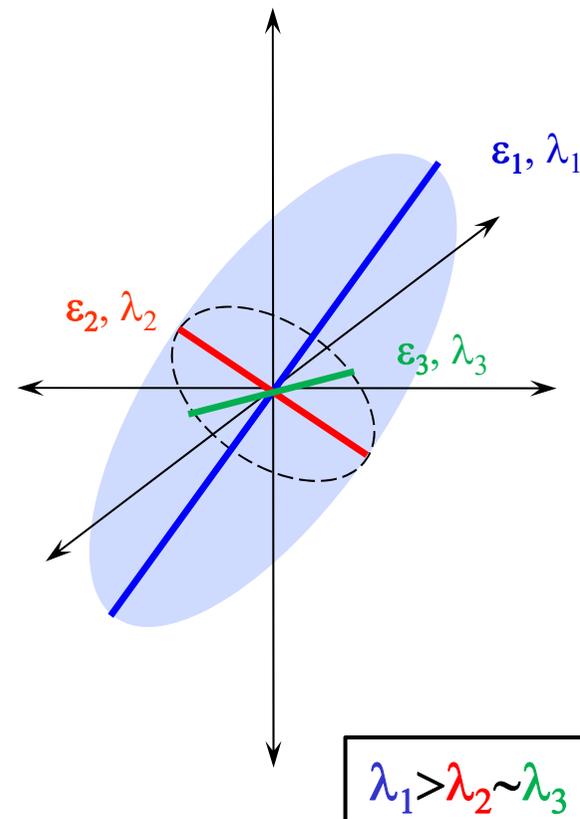
# Diffusion ellipsoid: eigenvalues & eigenvectors

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**Isotropic Diffusion**



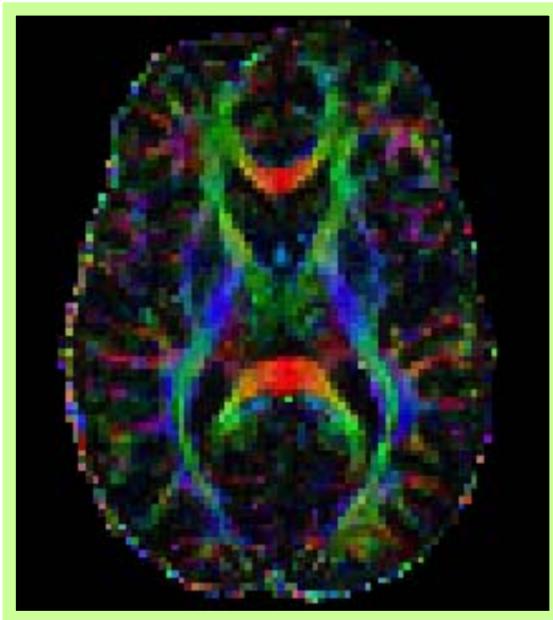
**Anisotropic Diffusion**



# Colour coded FA maps

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- Let  $\varepsilon_1$  designate the longest axis of the diffusion ellipsoid.
- $\varepsilon_1$  can be identified with the main direction of diffusion.
- This directional information can be added to the FA map using a colour code:



**Red** indicates directions in the  $x$  axis:  
right to left or left to right.

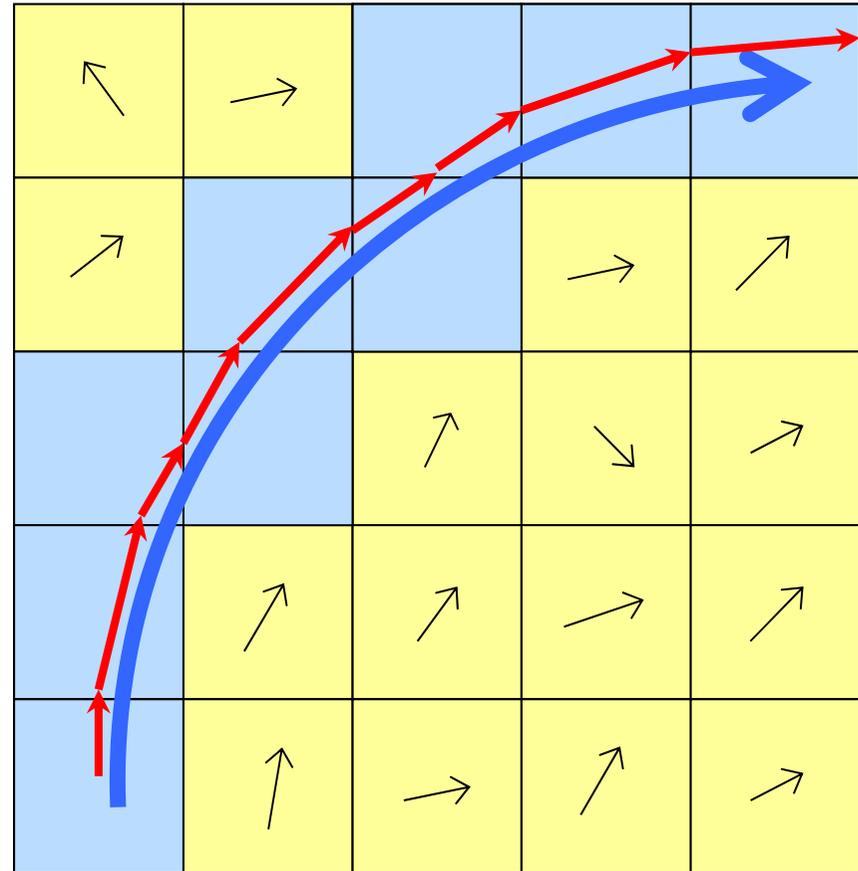
**Green** indicates directions in the  $y$   
axis: front to back or back to front.

**Blue** indicates directions in the  $z$  axis:  
foot-to-head direction or vice versa.

**Colour coded FA map.**

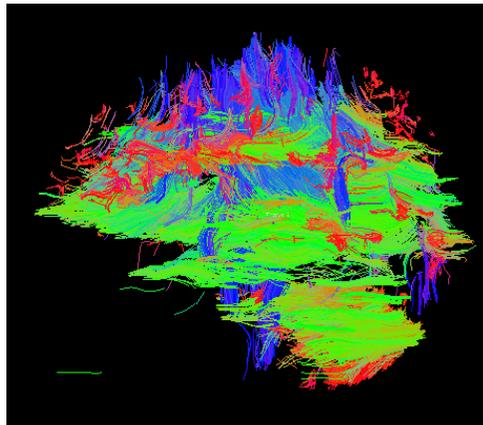
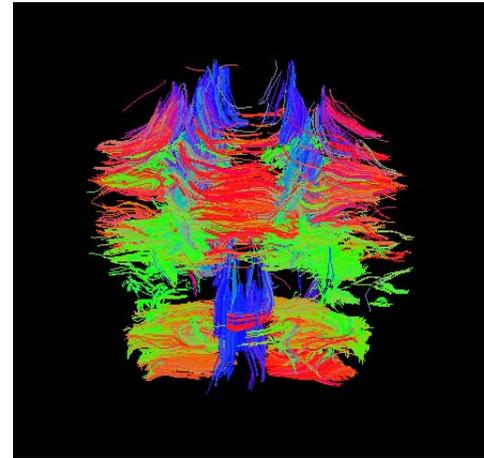
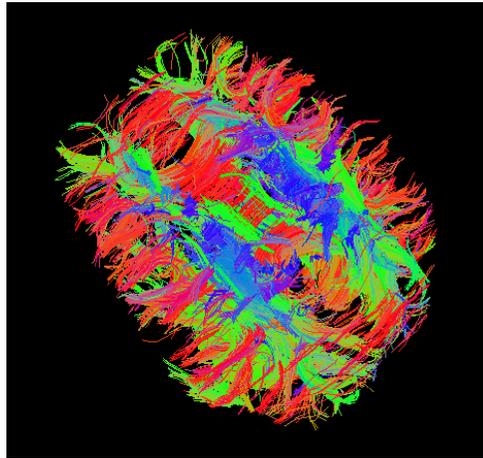
# Tractography

- Once direction  $\varepsilon_1$  has been calculated for all voxels, the trajectories of water molecules can be reconstructed using a method similar to the children's activity "connect the dots": we connect each voxel to the adjacent one toward which the fibre direction,  $\varepsilon_1$ , is pointing.



# Tractography in the Brain

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**Fibre tracks obtained for a dataset of a healthy volunteer using simple streamlining (FACT).**

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# Probabilistic Modeling of Diffusion MRI Signal

# Probabilistic Modelling

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- The information provided by DTI can be very useful for the characterisation of brain white matter.
- However, the estimated tensor can be highly dependent on noise.
- Probabilistic modelling can be used to estimate a probability distribution function (PDF) for the DTI model parameters.
- The standard deviation (s.d.) of this PDF is a good marker for confidence in the results.

# MCMC Methods (1)

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- Markov Chain Monte Carlo (MCMC) methods are based on Baye's Theorem:

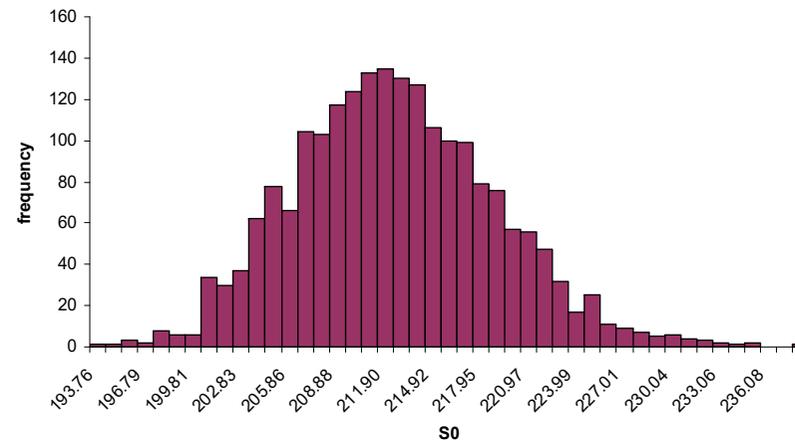
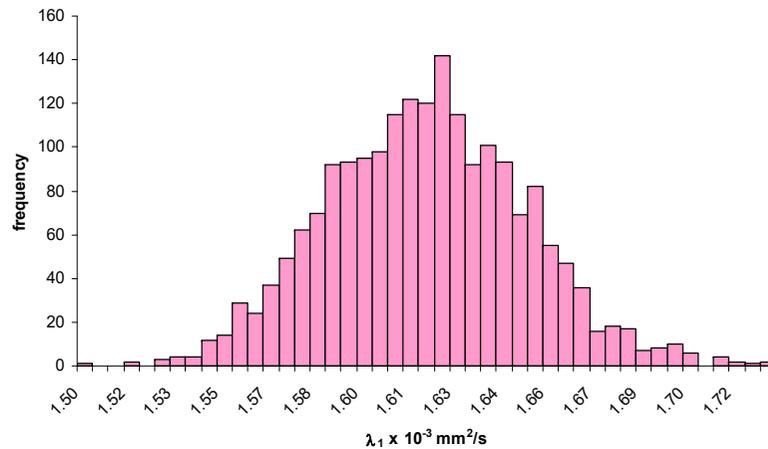
$$P(\omega | data) = \frac{P(data | \omega)P(\omega)}{P(data)}$$

where  $\omega$  represents the vector of model parameters.

- The prior term  $P(\omega)$  offers an opportunity for scientists to include knowledge they have about the expected values of the parameters.
- The term  $P(data | \omega)$  gives the probability of observing the data given a sampled set of parameters, and it is dependent on the model used.

# MCMC Methods (2)

- Instead of producing a single set of parameters MCMC methods produce a PDF for each parameter. For example:

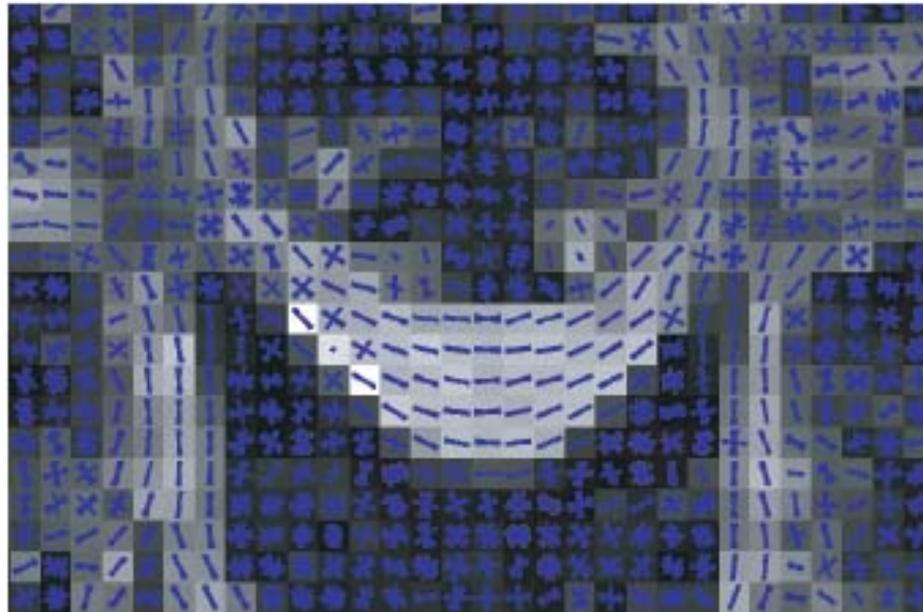


- The standard deviation of these PDFs is a good marker for confidence in the results.
- **FA maps, MD maps**, etc., can be obtained by taking the average of each PDF as the most likely value of the model parameters.

# PDF for fibre orientation

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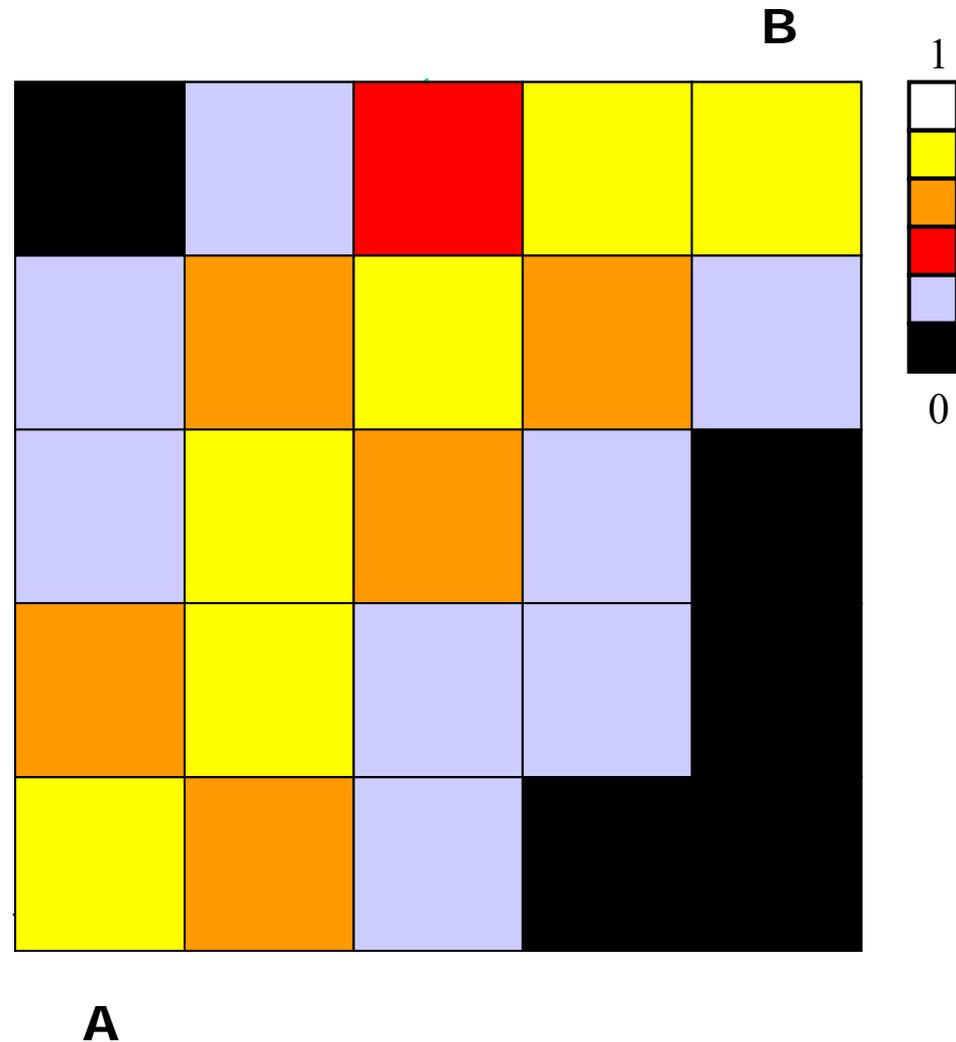
- For each voxel, we can obtain a PDF for the fibre orientation, by combining samples from the PDFs for  $\theta$  and  $\phi$ :



- Regions of one-fibre populations have very narrow distributions, while regions of crossing fibres show greater variability.

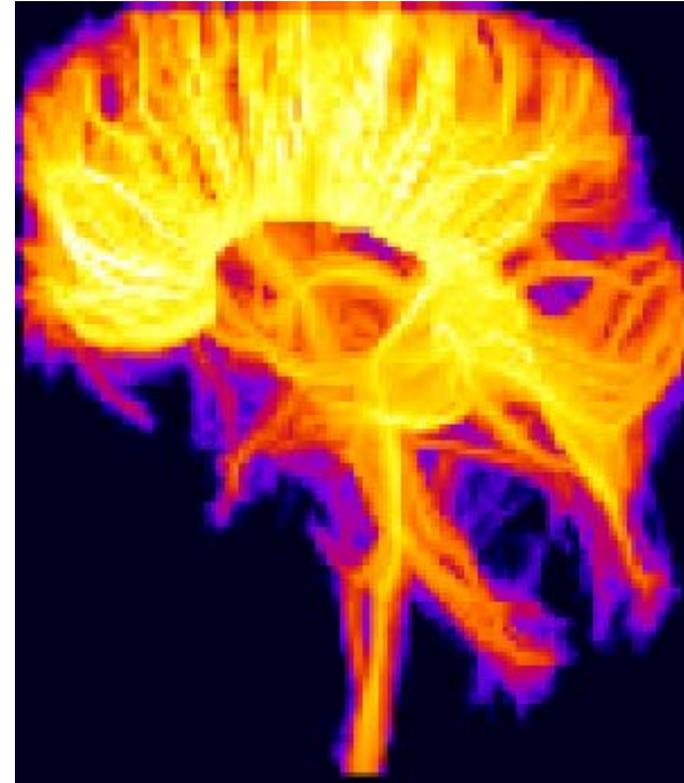
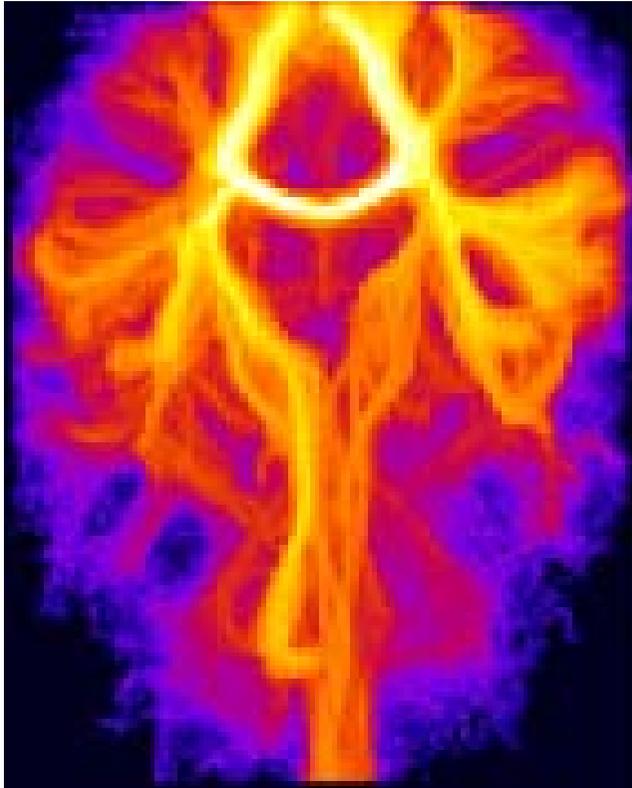
# Probabilistic Tractography

- For each sample of the directional PDF we can produce a track (or streamline).
- If we repeat this for a large number of samples, the probability of voxels A and B being connected can be calculated by dividing the number of streamlines that reach B, by the total number of streamlines generated from A.



# Probabilistic Tractography in the Brain

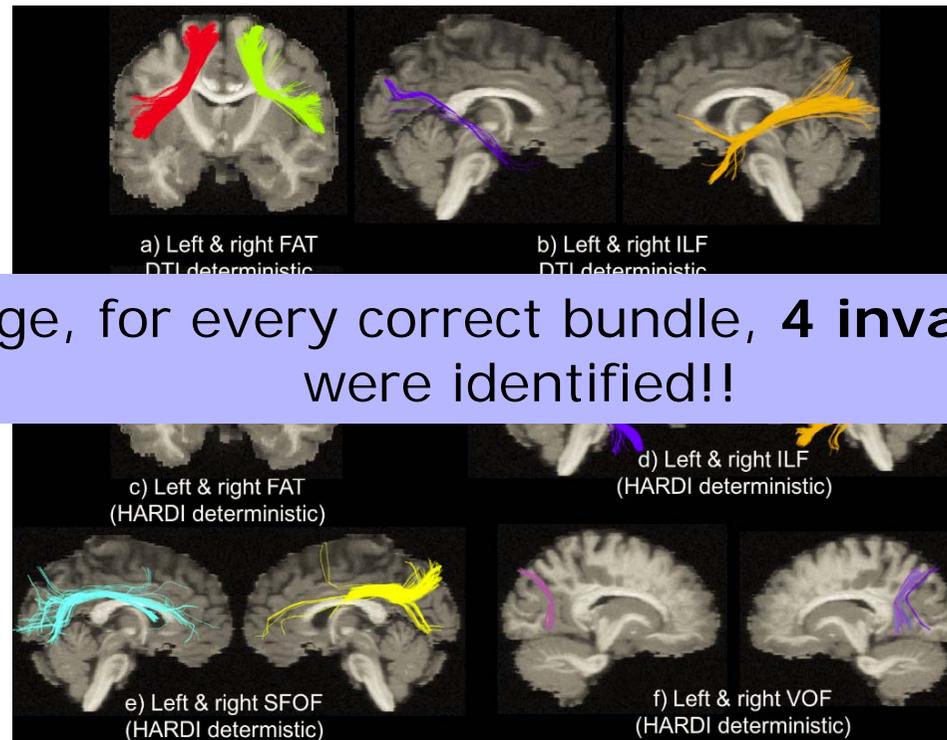
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**Probabilistic tractography dataset obtained for a healthy volunteer.**

# Tractography: A warning

- Examples of **invalid bundles**



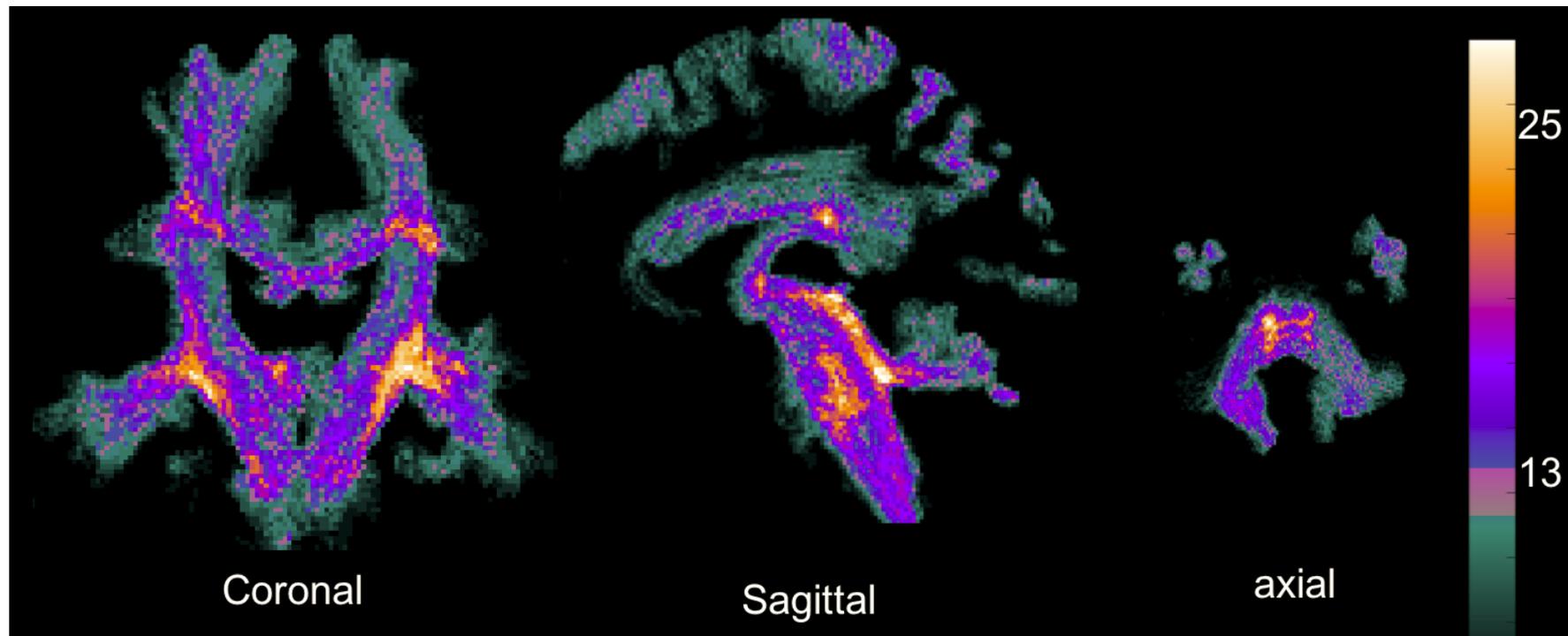
On average, for every correct bundle, **4 invalid bundles** were identified!!

| Bundles        | FAT | ILF | MLF | SFOF | VOF |
|----------------|-----|-----|-----|------|-----|
| Occurrence (%) | 88% | 85% | 95% | 81%  | 81% |

# Tractography: A warning

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- Most occurring locations of intersecting **invalid bundles**



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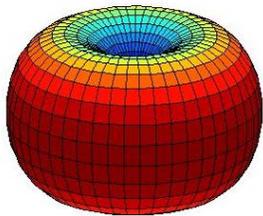
# Multiple fibres

## Beyond the Diffusion Tensor

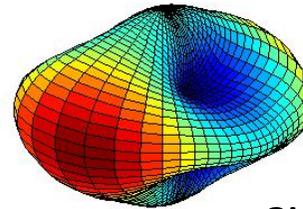
# Why the diffusion tensor is not the end of the story

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- DTI has a key limitation: it assumes a single fibre per voxel, and it cannot be used to explain the signal profile obtained from multiple crossing fibres.



Signal profile from a single fibre



Signal profile from two crossing fibres

- This limitation results in artificially low FA values in regions of crossing fibres, and in greater variability of FA and MD estimates.
- It is also a major obstacle for tractography and connectivity mapping, since the model fails at fibre crossings.
- A variety of alternative models and algorithms aim to resolve the orientations of crossing fibres.

# Multiple fibre approaches

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## **Model-Based Approaches**

- The multi-tensor model

## **Non-Parametric Approaches**

- Diffusion Spectrum Imaging (DSI)
- Q-ball Imaging
- Constrained Spherical Deconvolution (CSD)
- Persistent Angular Structure (PAS)

# The Multi-tensor Model (1)

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- The multi-tensor model is a simple generalisation of DTI, which replaces the single Gaussian model by a mixture of  $n$  Gaussian densities:

$$S(b, \vec{r}) = S_0 \sum_{i=1}^n f_i e^{-b \vec{r}^T \underline{D}_i \vec{r}}$$

where  $f_i$  represents the volume fraction of compartment  $i$ .

- This model assumes the number of distinct fibre populations,  $n$ , is known.
- Unlike the DTI model, the parameters  $\underline{D}_1, \dots, \underline{D}_n$  cannot be expressed as a linear function of the measurements, so the model fitting requires non-linear optimisation.

# The Multi-tensor Model (2)

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- Once fitted, the principal eigenvector of each  $\underline{D}_i$  provides a separate fibre orientation estimate.
- Practical considerations, such as the number of measurements and the noise level, limit the number of orientations the method can resolve reliably, and most studies use  $n=2$ .

## Acquisition requirements

- A minimum of  $n \times 7$  unique gradient directions are required to estimate the model parameters.
- In 2005 Alexander and Barker recommended using  $b$  in the range 2200-2800 s/mm<sup>2</sup>.

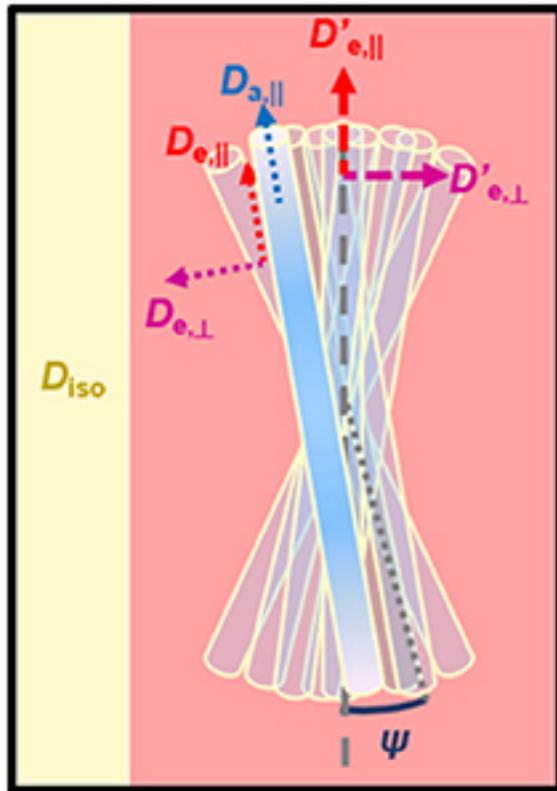
## Limitations

- Increased acquisition time and lower SNR.
- Using 64 directions the 2-tensor model can resolve 60 degree crossings, but does not consistently resolve 30 degree crossings.

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# Diffusion MRI and Microstructure

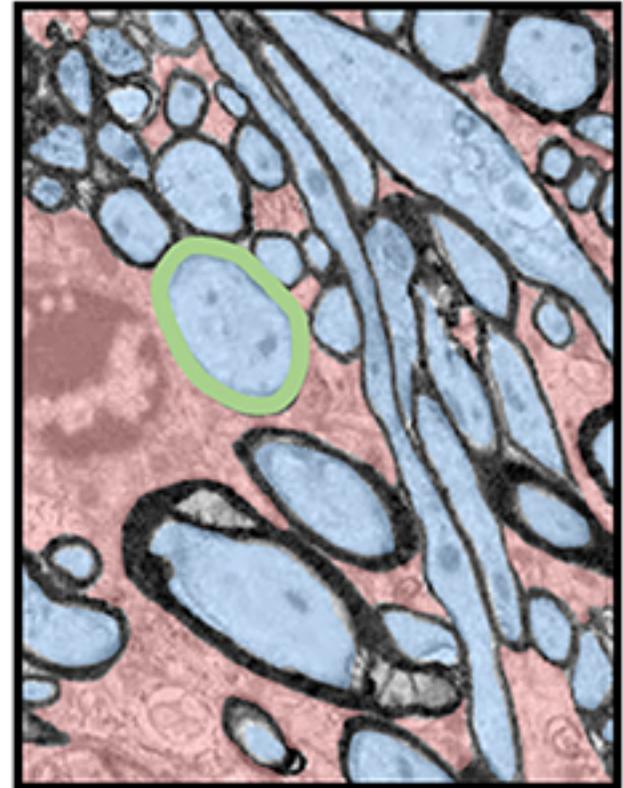
# Modelling multiple diffusion compartments



-  Intra-axonal space (IAS)
-  Extra-axonal space (EAS)
-  CSF
-  Myelin

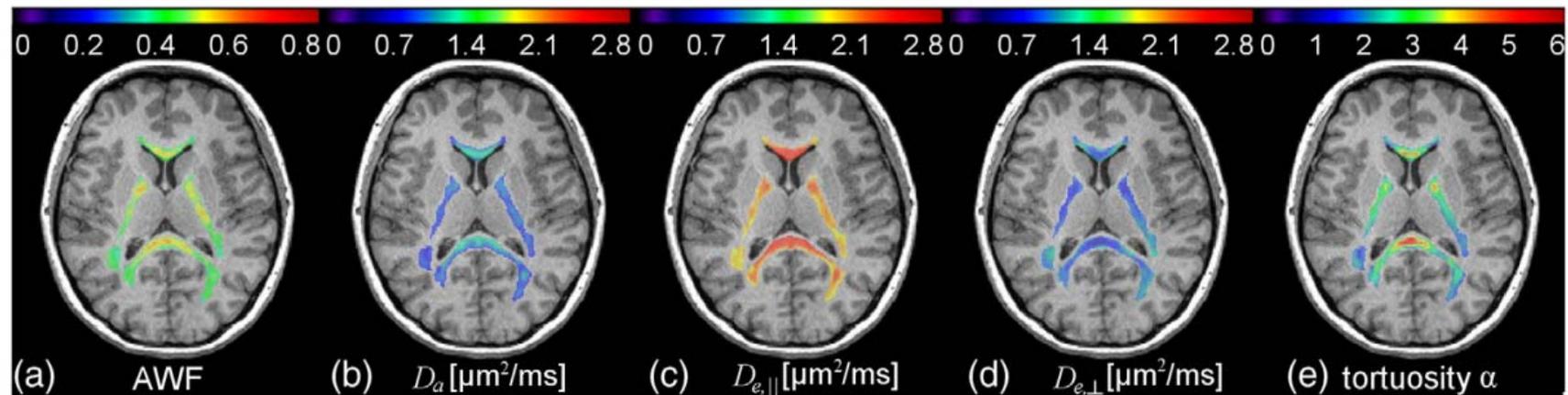
$$\frac{\text{Blue square}}{\text{Blue square} + \text{Red square}} = f_{intra}$$

$$\frac{\text{Blue square} + \text{Red square} + \text{Yellow square}}{\text{Blue square} + \text{Red square} + \text{Yellow square}} = f_{iso}$$

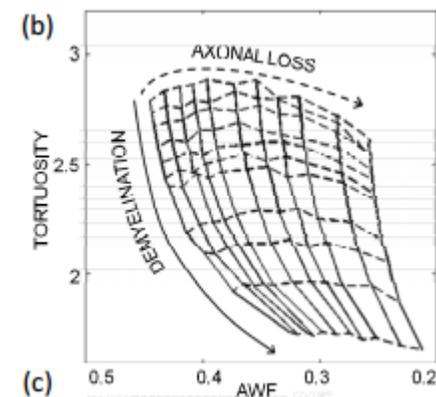


# White Matter Tract Integrity (WMTI)

- Introduced by Fieremans et al. (2011).

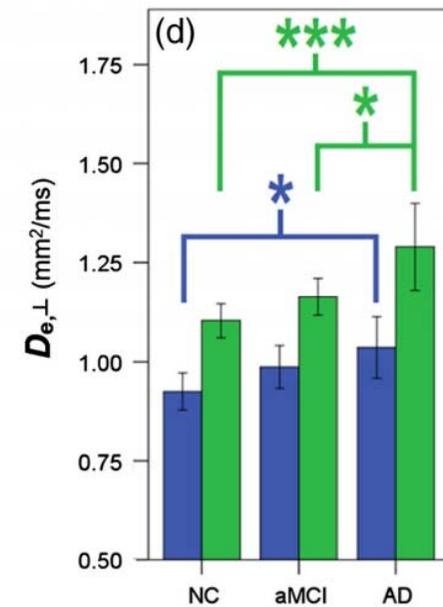
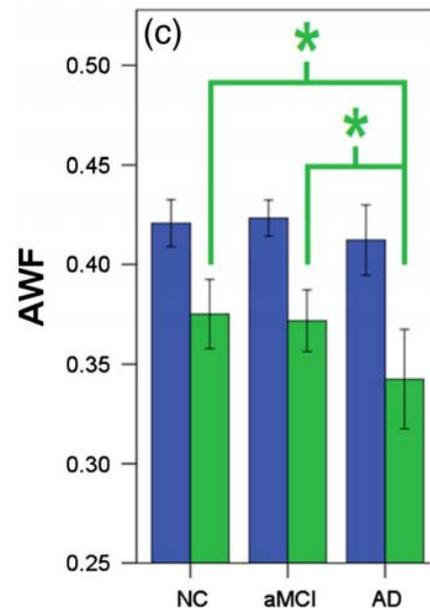
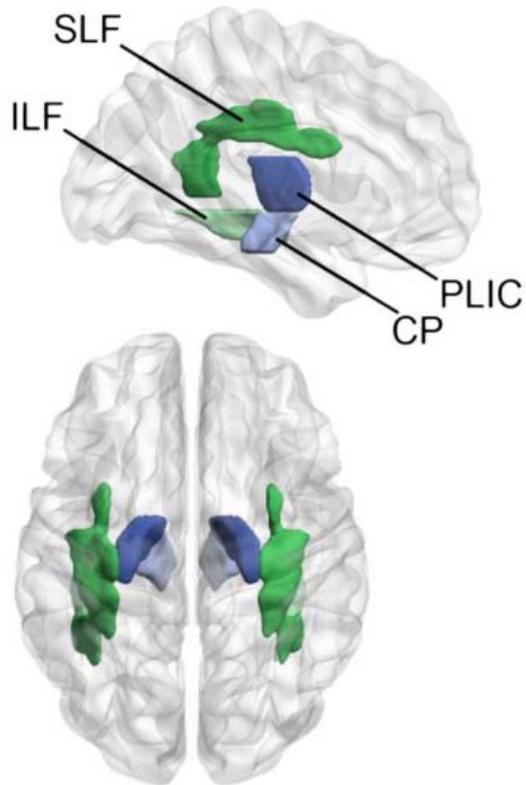


- AWF and tortuosity differentiate between axonal loss and demyelination (Fieremans et al. 2012).
- Typical acquisition time: 10-15 minutes (usually two b-values in the range 1000-2500  $\text{s}/\text{mm}^2$  x 30-60 directions).



# White Matter Tract Integrity (WMTI)

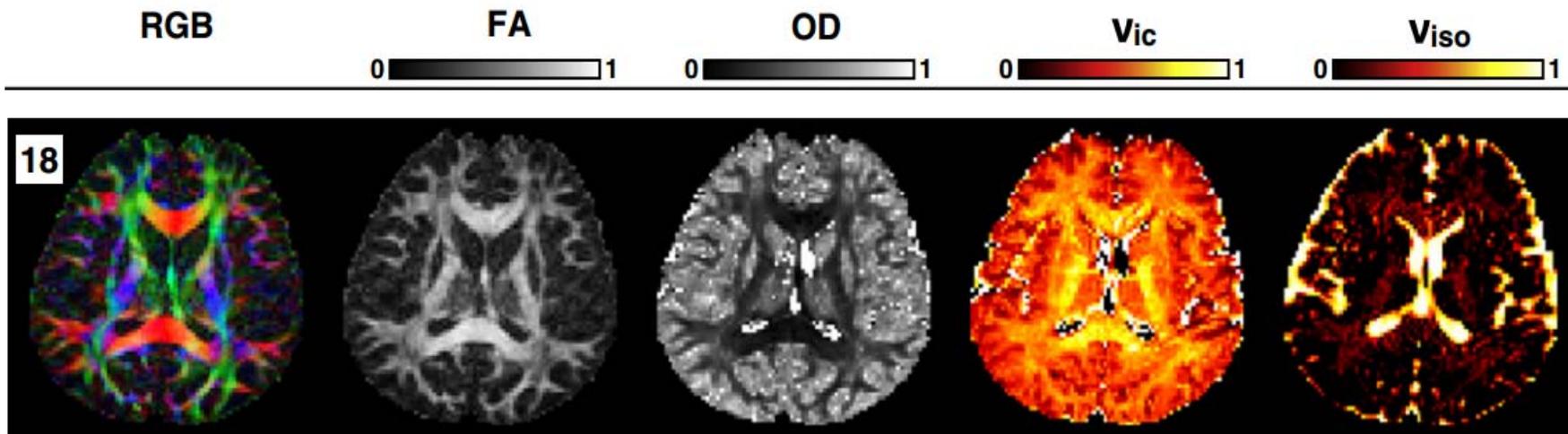
- WMTI metrics reflect differences between MCI and Alzheimer's disease (Benitez et al. 2014).



# Neurite Orientation Dispersion and Density Imaging (NODDI)

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- Introduced by Zhang et al. (2012).

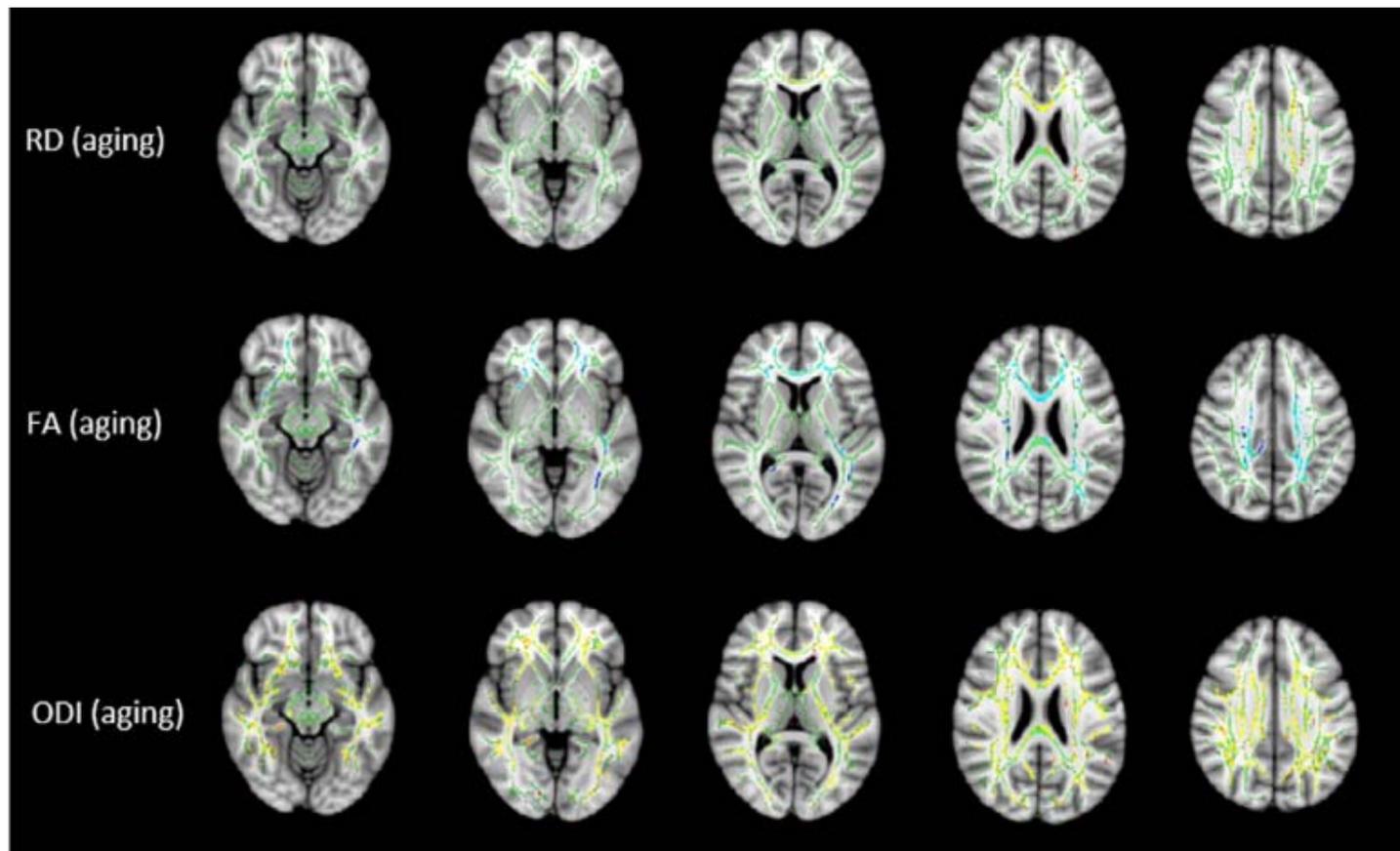


- Typical acquisition time: **30 minutes** ( $b=711\text{s/mm}^2 \times 30 \text{ dir}$ ,  $b=1000 \text{ s/mm}^2 \times 30 \text{ dir}$ ,  $b=2000\text{s/mm}^2 \times 60 \text{ dir}$ , and  $b=2855 \text{ s/mm}^2 \times 60 \text{ dir}$ ).

# Neurite Orientation Dispersion and Density Imaging (NODDI)

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- NODDI in young to middle-aged adults (Kodiweera et al. 2016).



# Summary

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- Tractography is a popular method used to reconstruct white matter fibre pathways.
- Easy to run, with multiple methods and software packages to choose from
- HOWEVER, this technique is severely affected by false positives and spurious findings, and results should be interpreted with scepticism.
- Advanced diffusion MRI acquisitions and modelling allows us to model multiple fibre orientations and multiple tissues types.
- There are many models to choose from with specific data acquisition requirements, so talk to your local MRI physicist if you are planning a diffusion experiment.

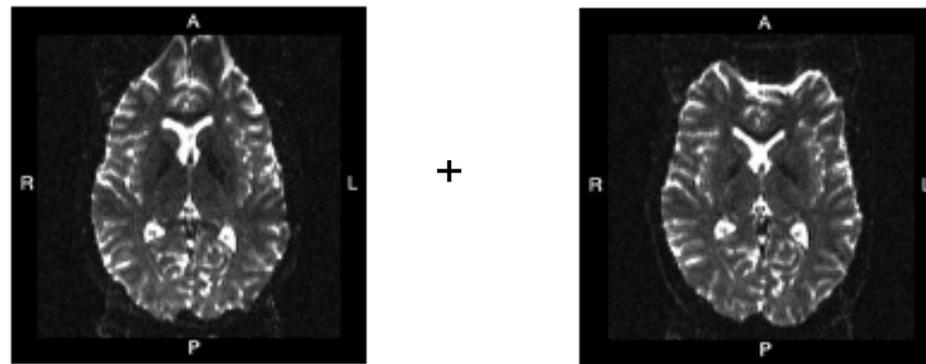
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# Hands on session

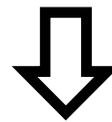
# Hands on Session

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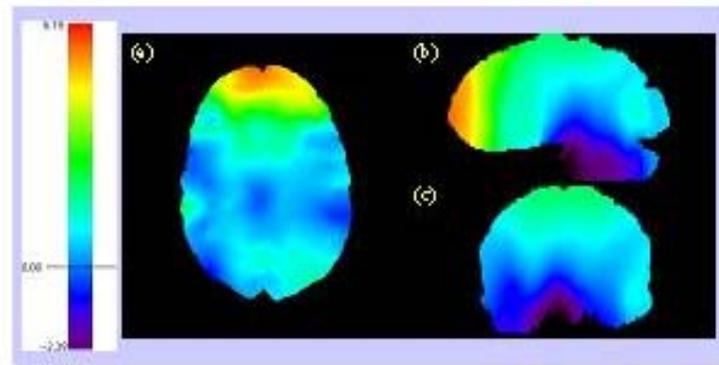
- **EPI distortion correction - TOPUP**



Phase encode  
direction P>>A



Phase encode  
direction A>>P



EPI distortion map.  
The colour coding  
shows the amount of  
displacement in pixel  
units.

# Hands on Session

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- **Group level analysis**
  - VBM style analysis
  - Tract based spatial statistics (tbss)
    - Pre-processing
    - Model fitting
    - Choose target + normalisation
    - Generate a white matter skeleton
    - Define design matrix and contrasts
    - Perform inference

